

Key

Name: \_\_\_\_\_

Date: \_\_\_\_\_

Arithmetic / Interest Final Exam Review

1) What are the following in terms of arithmetic sequences / series:

$n$  = number of terms

$t_n$  = value of the 'n<sup>th</sup>' term

$t_1$  = first term

$d$  = common difference

$S_n$  = sum of  $n$  terms

2) For the following arithmetic sequence, find the 47<sup>th</sup> term: 64, 61, 58, ...

$$t_1 = 64$$

$$t_n = t_1 + (n-1)d$$

$$d = -3$$

$$t_{47} = 64 + (47-1)(-3)$$

$$= -74$$

$$n = 47$$

$$= 64 + 46(-3)$$

3) Find the first term of an arithmetic sequence with  $t_{10} = 67$  and  $d = 7$ .

$$n = 10$$

$$t_n = t_1 + (n-1)d$$

$$t_{10} = 67$$

$$67 = t_1 + (10-1)(7)$$

$$t_1 = 4$$

$$d = 7$$

$$67 = t_1 + 63$$

4) If the first term of an arithmetic sequence is -42, and the last term is 54, with a common difference of 6, find the number of terms.

$$t_1 = -42$$

$$t_n = t_1 + (n-1)d$$

$$54 = 6n - 48$$

$$t_n = 54$$

$$54 = -42 + (n-1)6$$

$$6n = 102$$

$$d = 6$$

$$54 = -42 + 6n - 6$$

$$n = 17$$

5) Janie starts with 34 pins and adds 13 pins each month to her collection. How many pins will she have in 4 years? \*Think carefully about what your 'n' value will be.

34, 47, 60, ...

$$t_n = t_1 + (n-1)d$$

$$n = 49$$

$$t_5 = 34 + (49-1)(13)$$

$$t_1 = 34$$

$$t_5 = 34 + 624$$

$$d = 13$$

$$t_5 = 658$$

6) Ben is 12 and has a birthday party. Every 7 years after that, up to and including his 103<sup>rd</sup> birthday, he has another party. How many parties has Ben had in total?

$$\begin{array}{l}
 12, 19, 26, \dots, 103 \\
 t_1 = 12 \quad d = 7 \\
 t_n = 103
 \end{array}
 \quad
 \begin{array}{l}
 t_n = t_1 + (n-1)d \\
 103 = 12 + (n-1)(7) \\
 91 = 7(n-1)
 \end{array}
 \quad
 \begin{array}{l}
 n-1 = 13 \\
 n = 14 \\
 14 \text{ parties}
 \end{array}$$

7) Find the sum of the arithmetic series:  $57 + 50 + 43 + 36 + \dots + -34$

$$\begin{array}{l}
 t_1 = 57 \\
 d = -7 \\
 t_n = -34
 \end{array}
 \quad
 \begin{array}{l}
 t_n = t_1 + (n-1)d \\
 -34 = 57 + (n-1)(-7) \\
 -91 = -7(n-1) \\
 n-1 = 13
 \end{array}
 \quad
 \begin{array}{l}
 n = 14 \\
 S_n = \frac{n(t_1 + t_n)}{2} \\
 S_{14} = \frac{14(57 + -34)}{2}
 \end{array}
 \quad
 S_{14} = 161$$

8) Find the sum of an arithmetic series that starts at -8, has a common difference of -9, and has 21 terms.

$$\begin{array}{l}
 t_1 = -8 \\
 d = -9 \\
 n = 21
 \end{array}
 \quad
 \begin{array}{l}
 S_n = \frac{n}{2}(2t_1 + (n-1)d) \\
 S_{21} = \frac{21}{2}(2(-8) + (21-1)(-9))
 \end{array}
 \quad
 \begin{array}{l}
 S_{21} = 10.5(-16 + -180) \\
 S_{21} = 10.5(-196) \\
 S_{21} = -2058
 \end{array}$$

9) If an arithmetic series has  $S_{10} = 635$ , and  $t_{10} = 113$ , find  $t_1$ .

$$\begin{array}{l}
 S_n = \frac{n(t_1 + t_n)}{2} \\
 635 = \frac{10(t_1 + 113)}{2} \\
 t_1 + 113 = 127 \\
 t_1 = 14
 \end{array}
 \quad
 \begin{array}{l}
 635 = 5(t_1 + 113) \\
 t_1 + 113 = 127 \\
 t_1 = 14
 \end{array}$$

10) If an arithmetic series has a first term of 17, and  $S_9 = 729$ , find  $d$ .

$$\begin{array}{l}
 t_1 = 17 \\
 n = 9 \\
 S_9 = 729
 \end{array}
 \quad
 \begin{array}{l}
 S_n = \frac{n}{2}(2t_1 + (n-1)d) \\
 729 = \frac{9}{2}(2(17) + (9-1)d)
 \end{array}
 \quad
 \begin{array}{l}
 729 = 4.5(34 + 8d) \\
 162 = 8d + 34 \\
 128 = 8d \\
 d = 16
 \end{array}$$

11) Find  $\sum_{n=2}^7 3n + 2$

$$(3(2)+2) + (3(3)+2) + (3(4)+2) + (3(5)+2) + (3(6)+2) + (3(7)+2)$$

$$8 + 11 + 14 + 17 + 20 + 23$$

$$S_n = \frac{n(t_1 + t_n)}{2} \quad \left| \quad S_6 = \frac{6(31)}{2}$$

$$S_6 = \frac{6(8 + 23)}{2} \quad \left| \quad S_6 = 93$$

12) If you started with \$11 and then were given \$14 after the first minute, then \$17 after the next minute, and this pattern continued, how much would you have after 25 minutes?

$$\begin{array}{l}
 11 + 14 + 17 + \dots \\
 n = 26 \\
 t_1 = 11 \\
 d = 3
 \end{array}
 \quad
 \begin{array}{l}
 S_n = \frac{n}{2} [2t_1 + (n-1)d] \\
 S_{26} = \frac{26}{2} [2(11) + (26-1)(3)]
 \end{array}
 \quad
 \left. \begin{array}{l}
 S_{26} = 13(22+75) \\
 S_{26} = \$1261
 \end{array} \right|$$

\$1261

13) Calculate the simple interest when \$7500 is invested at 4.8% for 6 years.

$$\begin{aligned}
 I &= Prt \\
 I &= (7500)(0.048)(6)
 \end{aligned}$$

\$2160

14) Calculate the number of years (to the nearest tenth) that \$2800 is invested at 5% in order to make \$750 in simple interest.

$$\begin{aligned}
 I &= Prt & t &= \frac{750}{140} = 5.4 \\
 750 &= 2800(0.05)t \\
 750 &= 140t
 \end{aligned}$$

5.4 years

15) \$4800 is invested at 3.9% for 4 years simple interest. After 4 years, all of that money is taken and invested at 5.1% for 5 years simple interest. How much in total will you have after this?

$$\begin{aligned}
 I &= Prt & I &= 5548.80(0.051)(5) \\
 I &= 4800(0.039)(4) & I &= 1414.94 \\
 I &= 748.80 & \text{Total} &= 5548.80 + 1414.94 & \underline{\underline{\$6963.74}} \\
 4800 + 748.80 &= 5548.80
 \end{aligned}$$

16) \$35 000 is invested for 6 years at compound interest of 6.7%. How much total money will you have after 6 years?

$$\begin{aligned}
 A &= P(1+r)^t \\
 A &= 35000(1+.067)^6 \\
 A &= 35000(1.067)^6 \\
 A &= 51648.13 & \underline{\underline{\$51648.13}}
 \end{aligned}$$

17) Buddy ends up with \$28 600 after 6 years of compound interest at 4%. How much did he originally invest?

$$A = P(1+r)^t$$

$$28600 = P(1.04)^6$$

$$P = \frac{28600}{(1.04)^6} = 22603.00$$

\$22 603

18a) Cara wins \$3 000 000 in a lottery. She decides to invest it at 5.7% compound interest for 7 years. How much will she have in total at that point?

$$A = P(1+r)^t$$

$$A = 3000000(1.057)^7$$

\$4 422 279.28

b) How much more interest will she make with compound interest compared to if she invested with the same terms at simple interest?

$$I = Prt$$

$$I = 3000000(0.057)(7)$$

$$I = 1197000$$

$$\text{Total} = 3000000 + 1197000$$

\$4 197 000